
Reasoning at Scale: Why, How and What's Next.

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Datalog Reasoning with Trigger Graphs

	1B	2B	4B	8B	17B
Runtime (s)	203	226	520	993	2272
Memory (GB)	23	34	49	98	174
#IDPs	1B	2B	5B	10B	20B

Table: Reasoning over LUBM for 1B–17B of database triples.

Probabilistic Datalog Reasoning with Lineage Trigger Graphs

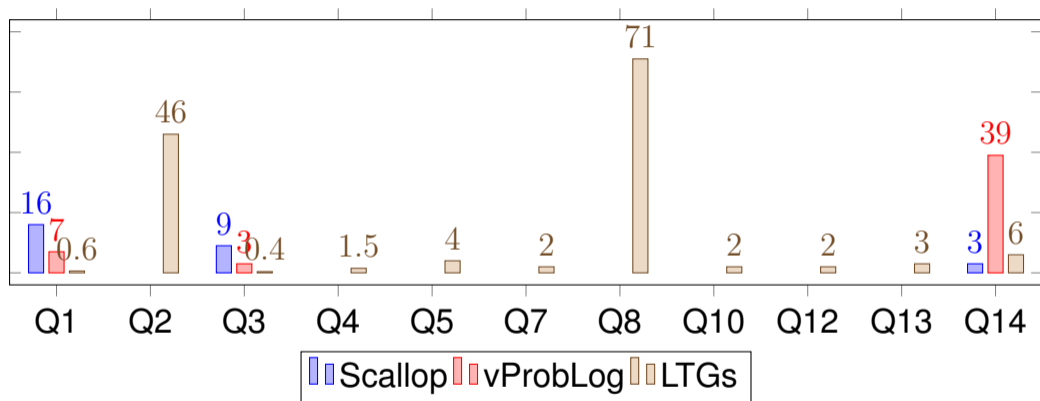


Figure: Time in seconds for goal-driven QA over probabilistic LUBM-100.

Reasoning (at Scale): Why

Why: Data Management

10/19/2014 10:00 AM
Five general Ontology companies show how it's done.

BY NATHAN NY, TERRY SUG, ANDREW JAIN, ROBERT HOGAN, KIM ALLEN, JEFFREY, AND JAMES TAYLOR

Industry-Scale Knowledge Graphs: Lessons and Challenges

Knowledge graphs are critical to many enterprises today. They provide the structure and context for knowledge that drive many products and make them more intelligent and "smarter."

In general, a knowledge graph describes subjects of interest and connections between them. For example, a knowledge graph may have nodes for a movie, the actors in that movie, the director, and so on. Each node may have properties such as an actor's name and age. There may be nodes for multiple movies involving a particular actor. The user can then traverse the knowledge graph to collect information on all the movies in which the actor appeared or, if applicable, directed.

Many general implementations require connections on the fly, so knowledge graphs relying on external data sources are often more complex and difficult to maintain. In fact, if you have a large number of connections, you may want to store them in a database. This is the case for the specific use cases of this paper. Building a large-scale knowledge graph for an enterprise is a complex task that has many challenges.

Knowledge graphs can be used in many ways. For example, they can be used to provide context for search results, to recommend related items, to analyze user behavior, and to track customer and employee interactions. In addition, they can be used to analyze user behavior and to track customer and employee interactions. In addition, they can be used to analyze user behavior and to track customer and employee interactions.

The data feeds at the knowledge graphs are often more complex, involving the collection and filtering of data from multiple sources and building out complex graphs, and designing the underlying algorithms to support the data.

While Microsoft's Bing knowledge graph and the Graph Knowledge Graph support search and security services based on data from external sources, other knowledge graphs are used for a variety of purposes, including personal knowledge graphs.

Whether for the world's largest search engines or for personal use, knowledge graphs are becoming increasingly important.

NewScientist Google's fact-checking bots build vast knowledge bank

The search giant is automatically building Knowledge Vault, a massive database that could give us unprecedented access to the world's facts

By Neil Hall

20 August 2014

f t g +



- Industry applications [21]
 - Microsoft and Google: search & QA.
 - Facebook: user recommendations.
 - Bosch: autonomous driving.
 - Samsung: healthcare.
 - LogicBlox: analytics.
- Success stories
 - RDFox.
 - Vadalog (acquired by Meltwater).

Why: Machine Learning

- Build simpler models [11].
 - The logical theory encodes prior knowledge– the neural model learns a simpler concepts.
- Train with fewer or even no data, e.g., zero-shot learning [8].
- Train in a weak fashion:
 - DeepProbLog [18]; Scallop [11].
 - NeuroLog [25]: abduction + WMC-based loss [4].

Efthymia Tsamoura and Loizos Michael **Neural-Symbolic Integration: a Compositional Perspective**. In AAI, pages 5051-5060, 2021.

Can we Learn via Weak Supervision Coming from Logic? Yes

(Work in progress)

Theorem

If \mathcal{G} is unambiguous and any $f \in \mathcal{F}$ is r -bounded, then we have:

$$\mathcal{R}^{01}(f) \leq O(\mathcal{R}_{\mathbb{P}}^{01}(f; \mathcal{G})^{1/M}) \quad \text{as } \mathcal{R}_{\mathbb{P}}^{01}(f; \mathcal{G}) \rightarrow 0$$

Furthermore, suppose $[\mathcal{F}]$ has a finite Natarajan dimension $d_{[\mathcal{F}]}$ and the function class $\{(\mathbf{y}, s) \mapsto 1\{\sigma'(\mathbf{y}) \neq s\} \mid \sigma' \in \mathcal{G}\}$ has a finite VC-dimension $d_{\mathcal{G}}$. Then, for any $\epsilon, \delta \in (0, 1)$, there is a universal constant C_4 such that with probability at least $1 - \delta$, the empirical partial risk minimizer with $\widehat{\mathcal{R}}_{\mathbb{P}}^{01}(f; \sigma) = 0$ has a classification risk $\mathcal{R}^{01}(f) < \epsilon$, if

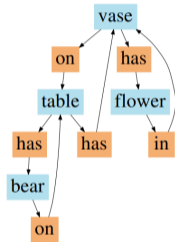
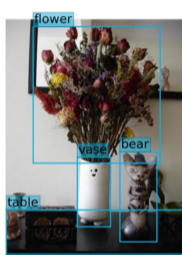
$$m_{\mathbb{P}} \geq C_4 \frac{c^{2M-2}}{r^M \epsilon^M} \left(((d_{[\mathcal{F}]} + d_{\mathcal{G}}) \log(6M(d_{[\mathcal{F}]} + d_{\mathcal{G}})) + d_{[\mathcal{F}]} \log c) \log \left(\frac{c^{2M-2}}{r^M \epsilon^M} \right) + \log \left(\frac{1}{\delta} \right) \right)$$

Believe in KRR

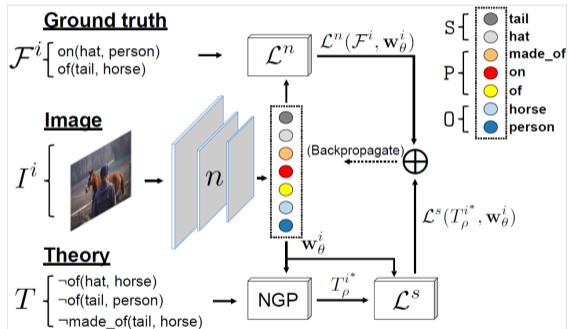
-My neurosymbolic research

Scene Graph Generation (AAAI 2023)

Task



Logic-Based Regularization



Davide Buffelli, and Efthymia Tsamoura. Scalable Theory-Driven Regularization of Scene Graph Generation Models. In AAAI, 2023.

Scene Graph Generation (AAAI 2023)

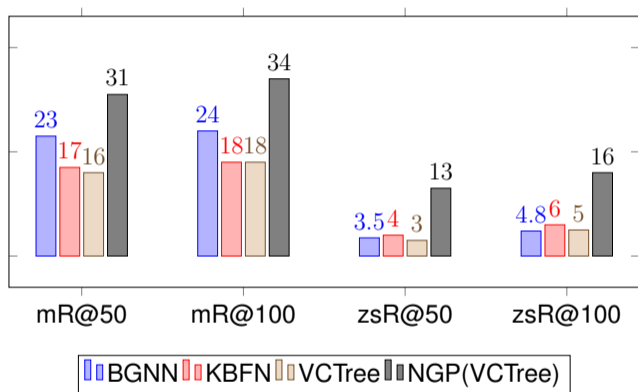


Figure: Comparison against BGNN [16], KBFN [10] and VCTree [22]. Benchmark: Visual Genome [13].

Scene Graph Generation (AAAI 2023)

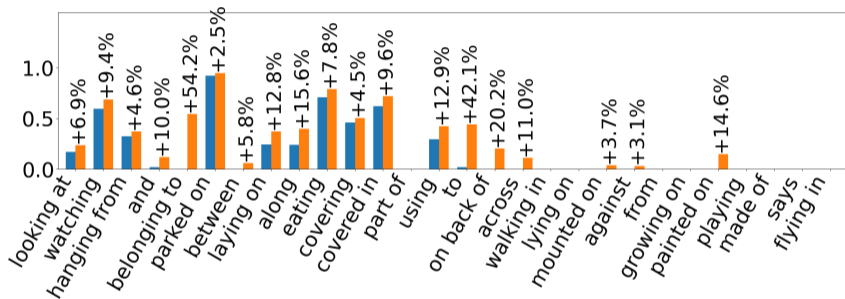
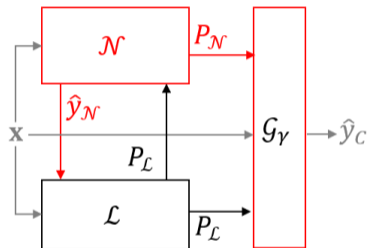


Figure: Recall of VCTree [22] on the 28 least frequent predicates: without NGP; with NGP. Benchmark: Visual Genome [13].

Knowledge Distillation into Deep Networks (ICML 2023)

Concordia



- First to support general first-order theories.
- Supports semi-/un-/supervised learning.

Operation	Equation
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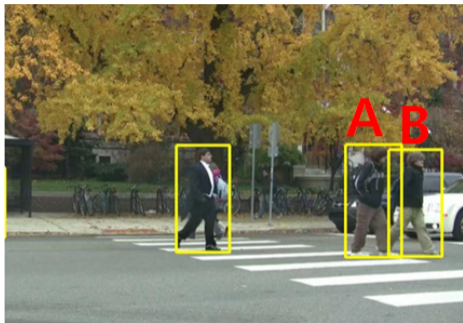
Inference	$\hat{\mathbf{y}} = \arg \max_{\mathbf{y}} P_{\mathcal{N}}(\mathbf{Y} = \mathbf{y} \mathbf{X} = \mathbf{x}, \boldsymbol{\theta})$
-----------	---

Training	$\hat{\boldsymbol{\theta}}_{t+1} = \arg \min_{\boldsymbol{\theta}} (\ell(\hat{\mathbf{y}}_{\mathcal{N}}, \mathbf{y}) + KL(P_{\mathcal{N}}, P_{\mathcal{L}}))$
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$$\hat{\boldsymbol{\lambda}}_{t+1} = \arg \max_{\boldsymbol{\lambda}} \prod_{(\mathbf{x}) \in \mathcal{D}} P_{\mathcal{L}}(\mathbf{X} = \mathbf{x}, \boldsymbol{\lambda}_t)$$

Leon Jonathan Feldstein, Jurčius Modestas and **Efthymia Tsamoura**. **Parallel neurosymbolic integration with Concordia**. In ICML (to appear), 2023.

Video Activity Detection (ICML 2023)



$SEQ(B_1, B_2) \wedge CLOSE(B_1, B_2) \rightarrow SAME(B_1, B_2)$

$DOING(B_1, A) \wedge SAME(B_1, B_2) \rightarrow DOING(B_2, A)$

Accuracy over 5 runs

Model	Avg (%)	Max (%)	Min (%)
ACD+ \mathcal{L} [17]	86.00	-	-
MobileNet	90.07	91.36	89.61
IARG(MobileNet) [14]	90.18	92.39	87.55
Concordia (MobileNet, \mathcal{L})	90.73	93.19	89.54
Inception	89.72	91.83	86.84
IARG(Inception) [14]	88.88	91.67	85.33
Concordia (Inception, \mathcal{L})	92.75	93.34	92.31

Leon Jonathan Feldstein, Jurčius Modestas and **Efthymia Tsamoura**. **Parallel neurosymbolic integration with Concordia**. In ICML (*to appear*), 2023.

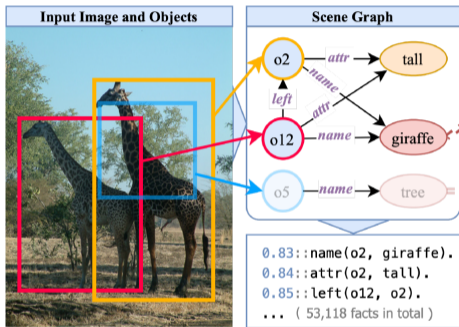
Entity Linking (ICML 2023)

Table: Results on entity linking.

Model	F_1	Acc (%)
BERT (sp)	0.88	88.5
Concordia(BERT) (sm)	0.91	91.4

Leon Jonathan Feldstein, Jurčius Modestas and **Efthymia Tsamoura**. **Parallel neurosymbolic integration with Concordia**. In ICML, 2023 (*to appear*).

Visual QA (SIGMOD 2023)



$Q(O) \leftarrow \text{NAME}(\textit{herbivore}, O)$
 $\text{NAME}(N, O) \wedge \text{NAME}(N', O) \rightarrow \text{ISA}(N', N)$
 $\rightarrow \text{ISA}(\textit{giraffe}, \textit{herbivore})$
 $\rightarrow \text{ISA}(\textit{deer}, \textit{herbivore})$

Table: Recall@5 on VQAR [11].

Testset	LXMERT [24]	RVC [7]	TG-Guided VQA
C5	64.05%	74.62%	87.01%
C6	56.51%	72.04%	85.45%

Efthymia Tsamoura, Jaehun Lee, and Jacopo Urbani. **Probabilistic Reasoning as Scale: Trigger Graphs to the Rescue.** In SIGMOD, 2023 (to appear).

How this Reasoning Journey Started

Benchmarking the Chase (PODS 2017)

Benchmarking the Chase

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ABSTRACT

The chase is a family of algorithms used in a number of data management tasks, such as data exchange, answering queries under dependencies, query reformulation with constraints, and data cleaning. It is well established as a theoretical tool for understanding these tasks, and as a building block of prototype systems that have been developed. While individual chase-based systems and particular optimizations of the chase have been experimentally evaluated in the past, we provide the first comprehensive and publicly available benchmark, with implementation and source code repositories, for evaluating chase implementations across a wide range of scenarios about the dependencies used by the chase. We used our benchmark to compare chase-based systems on data exchange and query answering tasks with one another, as well as with systems that can solve similar tasks by avoiding the chasing algorithm completely. Our results indicate that avoiding the chasing algorithm completely can evaluate queries with a number of non-trivial constraints, but the factors that impact the performance of chase implementations.

1. INTRODUCTION

The chase [25] is a data-manipulation technique developed by the database community for reasoning with constraints, also known as dependencies, expressed as normal implications possibly containing existential quantification in the conclusions. When applied to a set of dependencies and a set of facts, the chase entails the task to force self-joining in order to satisfy the dependencies.

The chase has been extensively studied in a theoretical context over the last decade through various, such as developing optimizations of the chase algorithm, and building chase-based systems for various tasks, such as query answering, foreign key propagation, or change propagation in graph dependencies. In this paper, we present a public benchmark to evaluate the performance of chase implementations on large sets of complex dependencies and large instance domain instances. This suggests that it is time to evaluate the extent to which competing chase-based systems are practically feasible.

The chase is closely related to and can be seen as a special case of foreign key propagation, which is well understood, and it can also be seen as a generalization of standard query evaluation in

database. But while the former proving and the database computation have a long history of existing benchmarks and detailed evaluation methodologies (e.g., [24, 23, 22] and [17, 14] in the context of the TPC-H [18] and the TPC-DS [19] benchmarks), such a task, conceptualized by identifying the right experimental conditions, is still missing in the chase for the database research and data management.

This paper aims to take a major step in changing this situation. We present a new benchmark for chase systems covering a wide range of scenarios. Next, the systems in the benchmark support different levels of dependencies, we have developed algorithms with different structural properties, and diverse ways of solving them.

We also discuss simple tasks for two main applications of the chase: (1) data exchange, which involves maintaining an instance of a target schema satisfying a given set of dependencies with respect to an instance of a source schema, and (2) computing certain answers to conjunctive queries over databases with dependencies. We then address a variety of publicly available systems as our benchmark in order to answer the following questions:

- How do existing chase-based systems fare in database terms on these tasks? That is, to what extent can they be considered as practical for the chase-based approaches to solving these tasks are practically feasible?

- What operations, and structural devices are most critical for the performance of chase-based systems?

- Are there other approaches or other kinds of systems that can perform these same tasks and, if so, how do they compare to tasks that are the chase?

In an attempt to answer these questions, we considered a number of systems that tackle these tasks as a composition, including systems tailored from data exchange, data cleaning, query reformulation, and query answering.

We considered three main configurations: we included each system, similar to the chase, and we performed a data exchange and query answering. We tried to ensure that the constraints with the related dependencies, we also applied our benchmark to systems that are not specifically “tailored” to chase systems, but that can manipulate patterns some of the tasks that the chase addresses. In particular, we looked at finding regular graph regular functions, which can solve both data exchange and query answering problems, as well as finding theorem provers that can solve certain query answering problems.

Regarding the rest of this paper, we first present some background about the chase (Sections 2 and 3). Next, we describe our benchmark (Section 4), and discuss the design, implementation, and test scenarios (Section 5). Then, we present the system configurations (Section 6), followed by a discussion of the results (Section 7) and the future challenges that emerged from our study (Section 8). Finally, we close with a discussion of the re-

- Tasks
 - Materialization.
 - Query answering.

- (Some) Engines
 - RDFox [20].
 - DLV [15].
 - E [23].
 - Graal [1].
 - Pegasus [19].

Michael Benedikt, George Konstantinidis, Giansalvatore Mecca, Boris Motik, Paolo Papotti, Donatello Santoro, and **Efthymia Tsamoura**. Benchmarking the Chase. In PODS, pages 37–52, 2017.

Benchmarking the Chase (PODS 2017)

Benchmarking the Chase

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Oxford, UK Potenza, Italy Pogradec, ALB

ABSTRACT

The chase is a family of algorithms used in a number of data management tasks, such as data exchange, answering queries, query decomposition, query reformulation with constraints, and data cleaning. It is well established as a theoretical tool for understanding these tasks, and as a building block of practical systems that have been developed. While individual chase-based systems and practical optimizations of the chase have been experimentally evaluated in the past, we provide the first comprehensive and publicly available benchmark—our benchmark and several optimizations—for evaluating chase implementations across a wide range of scenarios that the algorithms used the chase. We used our benchmark to compare chase-based systems on data exchange and query answering tasks with one another, as well as with competitors that use more standard logic programming or query optimization. Our evaluation provides us with a number of new insights concerning the factors that impact the performance of these implementations.

1. INTRODUCTION

The chase [25] is a logic-programming technique developed by the database community for reasoning with constraints, also known as dependencies, expressed as normal implications possibly containing existential quantification in the conclusions. When applied to a set of dependencies and a set of facts, the chase entails the facts in a forward-chaining manner to satisfy the dependencies. The chase has been extensively studied in a theoretical context over the last decade practical aspects, such as developing optimizations of the chase algorithms and building chase-based systems for various tasks, have given rise to considerable research efforts in chasing systems to support applications beyond classical logic programming, with applications in satisfiability, hardware verification, query rewriting, etc. The performance of chase implementations in large sets of complex dependencies and large instance domains, however, has not been thoroughly studied. This suggests that it is time to evaluate the extent to which computing the chase is practically feasible.

The chase is clearly intended to end user as a special case of reasoning, which leads to software and hardware, and so can also be seen as a generalization of standard query evaluation in Relational Databases. In fact, a large part of the work in practice is concerned with the problem of query evaluation in the presence of constraints, and the chase is a natural way to think about this problem. In this paper, we provide a comprehensive evaluation of the chase in a number of practical scenarios. We use our benchmark to compare chase-based systems with one another, as well as with competitors that use more standard logic programming or query optimization. Our evaluation provides us with a number of new insights concerning the factors that impact the performance of these implementations.

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database. But while the theory proving and the database communities have a long history of creating benchmarks and shared evaluation methodologies (e.g., [25], [20], [21] and [17], [18]) in the context of the chase [25] (the latter, being a more conceptual approach), there has been no systematic effort to create a benchmark for evaluating the performance of practical implementations to support applications in satisfiability, hardware verification, query rewriting, and data management.

This paper aims to take a major step in bridging this missing link in the chase: the creation of a public, available, and well-motivated benchmark for these systems covering a wide range of scenarios. These are scenarios in the literature support all seven kinds of dependencies, we have developed algorithms over with different structural properties, and diverse set of chasing rules.

We also discuss in-depth tasks for two main applications of the chase: (1) data exchange, which involves identifying an instance of a target schema satisfying a given set of dependencies with respect to an instance of a source schema, and (2) computing certain answers to conjunctive queries over databases with dependencies. We then address a variety of publicly available systems on our benchmark in order to answer the following questions:

- How do existing chase-based systems fare in database terms on these tasks? That is, to what extent can they be considered an ideal for the chase-based approaches to solving these tasks are practically feasible?
- What operations, and architectural choices are most critical for the performance of chase-based systems?
- Are there other approaches or other kinds of systems that can perform these same tasks end, if so, how do they compare to each other for the chase?

In an attempt to answer these questions, we considered a number of variants that highlight the chase as a constraint, including query rewriting, data cleaning, query reformulation, and query answering.

We extended the state-of-the-art implementations used in each experiment (either in the chase, or not) to perform similar to data exchange and query answering. We then used our benchmark to compare with the related competitors, we also applied our benchmark to systems that are not specifically “tailored” at chase tasks, but that can nonetheless perform some of the tasks that the chase addresses. In particular, we looked at Datalog and logical query optimization systems as they can solve both data exchange and query answering problems, as well as a leading theorem prover (an solver system) query answering problems.

Organization. In the rest of this paper, we first present some background about the chase (Sections 2 and 3). Next, we describe our benchmark (Section 4), and discuss the settings, dependencies, and test scenarios (Section 5). Then, we present the system performance results (Section 6), followed by a discussion of the insights gained (Section 7), and the future challenges that emerged from our study (Section 8). Finally, we close with a discussion of the re-

– Paper takeaways

- Equality is challenging.
- Dictionary encoding played a role.
- Chase engines could support “realistic” scenarios.

– Practitioners’ takeaways

- Chase engines were struggling with ~100M facts and few hundreds of rules.
- LUBM-1k was only supported by one engine running on multiple cores.

Michael Benedikt, George Konstantinidis, Giansalvatore Mecca, Boris Motik, Paolo Papotti, Donatello Santoro, and **Efthymia Tsamoura**. **Benchmarking the Chase**. In PODS, pages 37–52, 2017.

How this Journey Started (cont’): ProbLog

Under consideration for publication in Theory and Practice of Logic Programming 1

Inference and Learning in Probabilistic Logic Programs using Weighted Boolean Formulas

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submitted 26 June 2012; revised 01 January 2013; accepted 07 March 2013

Abstract

Probabilistic logic programs are logic programs in which some of the facts are annotated with probabilities. This paper investigates how classical inference and learning tasks known from the graphical model community can be tackled for probabilistic logic programs. Several such tasks such as computing the marginals gives evidence and learning from partial interpretations have not really been addressed for probabilistic logic programs before.

The first contribution of this paper is a suite of efficient algorithms for various inference tasks. It is based on a combination of the program and the queries and evidence to a weighted Boolean formula. This allows us to reduce the inference tasks to well-studied tasks such as weighted model counting, which can be solved using state-of-the-art methods known from the graphical model and knowledge compilation literature. The second contribution is an algorithm for parameter estimation in the learning from interpretations setting. The algorithm employs Expectation Maximization, and is built on top of the developed inference algorithms.

The proposed approach is experimentally evaluated. The results show that the inference algorithms improve upon the state-of-the-art in probabilistic logic programming and that it is indeed possible to learn the parameters of a probabilistic logic program from interpretations.

KEYWORDS: Probabilistic logic programming, Probabilistic inference, Parameter learning

1 Introduction

There is a lot of interest in combining probability and logic for dealing with complex relational domains. This interest has resulted in the fields of Probabilistic Logic Programming (PLP) (De Raedt et al. 2008) and Statistical Relational Learning (SRL) (Getoor and Taskar 2007). While the two fields essentially study the same problem, there are differences in emphasis. SRL techniques have focused on the estimation of probabilistic graphical models like Markov or Bayesian networks with

– Why ProbLog [6]

- Support Web-crawled KBs.
- Reasoning over deep neural classifiers.
- Clean semantics.

– State of affairs

- Limited applicability.
- Could not support LUBM-1.
- **Contribution**
 - Datalog techniques + provenance semirings.
 - Improved scalability by 100x.

Efthymia Tsamoura, Victor Gutierrez-Basulto, and Angelika Kimmig. Beyond the Grounding Bottleneck: Datalog Techniques for Inference in Probabilistic Logic Programs. In AAAI, pages 10284-10291, 2020.

Reasoning at Scale: How -Trigger Graphs

Efthymia Tsamoura, David Carral, Enrico Malizia, and Jacopo Urbani. **Materializing Knowledge Bases via Trigger Graphs**. In VLDB, pages 943-951, 2021.

Trigger Graphs: Why

- **Key to support goal-driven QA over transitive rules.**
- **Standard bottom-up evaluation:**
 - may derive logically redundant facts;
 - may try to execute rules that derive no facts.
- **The above negatively impact the runtime and the memory.**

How: Trigger Graphs

Rules

$$r(X, Y) \rightarrow R(X, Y) \quad (r_1)$$

$$R(X, Y) \rightarrow T(Y, X, Y) \quad (r_2)$$

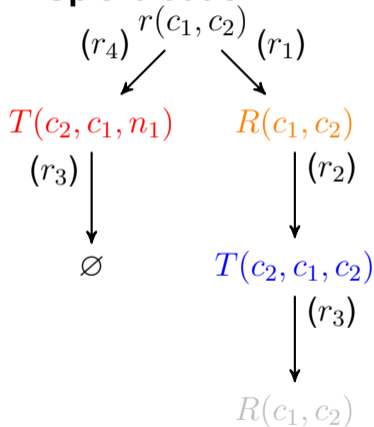
$$T(Y, X, Y) \rightarrow R(X, Y) \quad (r_3)$$

$$r(X, Y) \rightarrow \exists Z. T(Y, X, Z) \quad (r_4)$$

Facts

$$\rightarrow r(c_1, c_2)$$

Bottom-Up evaluation



How: Trigger Graphs

Rules

$$r(X, Y) \rightarrow R(X, Y) \quad (r_1)$$

$$R(X, Y) \rightarrow T(Y, X, Y) \quad (r_2)$$

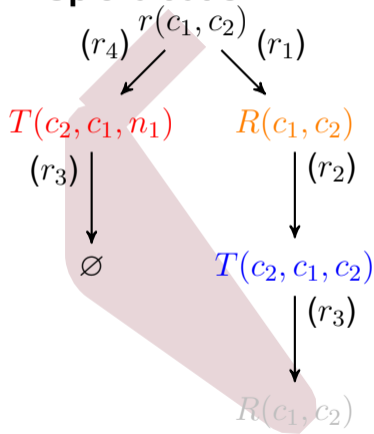
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Bottom-Up evaluation



How: Trigger Graphs

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$$r(X, Y) \rightarrow R(X, Y) \quad (r_1)$$

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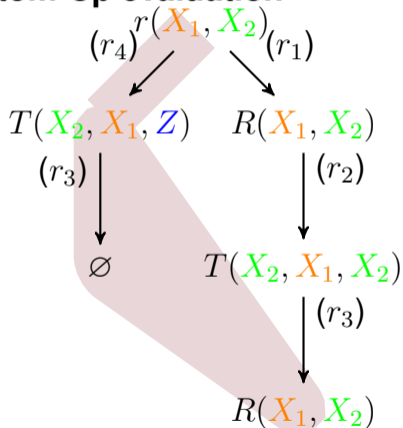
$$T(Y, X, Y) \rightarrow R(X, Y) \quad (r_3)$$

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Facts

$$\rightarrow r(c_1, c_2)$$

Bottom-Up evaluation



How: Trigger Graphs

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$$r(X, Y) \rightarrow \exists Z. T(Y, X, Z) \quad (r_4)$$

Facts

$$\rightarrow r(c_1, c_2)$$

Trigger graph



Trigger graph-based reasoning

TGs delineate the rule executions

- Execute r_1 over the input instance.
- Execute r_2 over the derivations of r_1 .
- **No other operation is taking place.**

Important to node

- Facts are stored inside the nodes, i.e., not stored in a single set like in all bottom-up engines.
- This data separation makes joins run faster.

Trigger graph



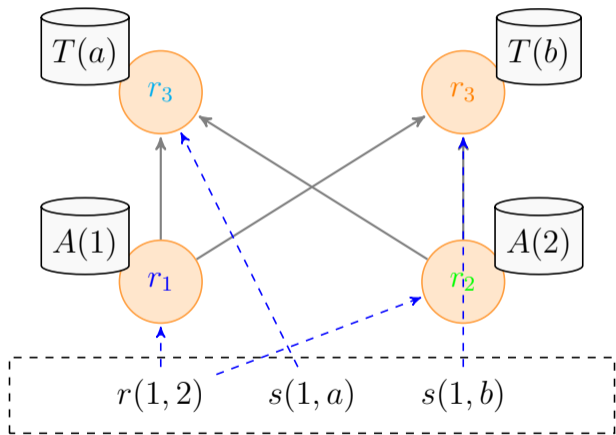
Trigger graph-based reasoning

Rules

$$r(X, Y) \rightarrow A(X) \quad (r_1)$$

$$r(X, Y) \rightarrow A(Y) \quad (r_2)$$

$$A(X) \wedge s(X, Z) \rightarrow T(Z) \quad (r_3)$$



Trigger Graphs for Linear Rules

- **Phase I: Static TG Computation.**
 - Compute a *representative* instance B^* , i.e., one that captures *all* possible rule execution paths.
 - Compute a *plan* G that mimics the rule execution when reasoning over B^* .
- **Phase II: Redundancy Elimination.**
 - Eliminate nodes that lead to redundant facts (via detecting preserving homomorphisms).
- **Phase III: Reasoning.**
 - The computed TG can be used to reason over *all* input instances.

Trigger Graphs for Linear Rules: Complexity

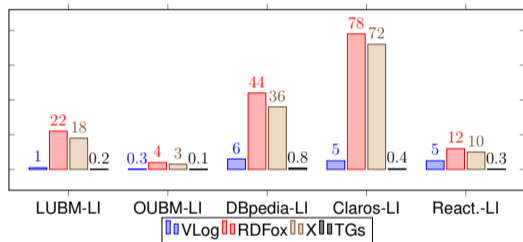
Let P be a linear program that admits a finite universal model.

Theorem (Complexity)

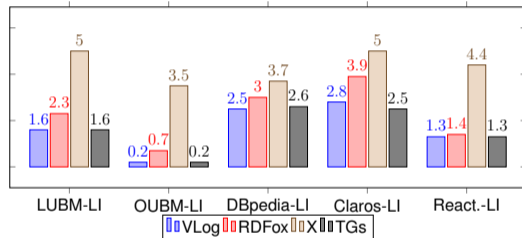
Computing a TG for P is double exponential in P . If the arity of the predicates in P is bounded, the computation time is (single) exponential.

Reasoning over Linear Rules

Total materialization times in s



Pick memory in GB



Trigger Graphs for Datalog Rules

TGs for Linear Rules

- Static TG computation.
- Use the pre-computed TG to reason over *all* instances.
- Redundancy elimination via detecting preserving homomorphisms.

TGs for Datalog Rules

- Interleave TG creation with reasoning.
- The computed TG can be used to reason over the given instance only.
- Redundancy elimination via query containment [3].

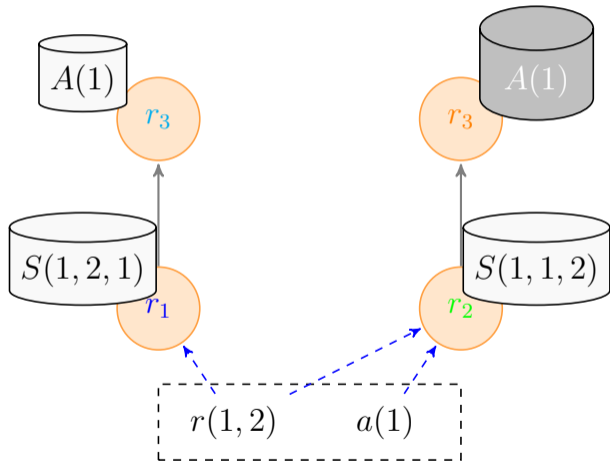
Trigger Graphs for Datalog Rules: Example

Rules

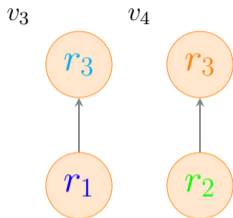
$$r(X, Y) \rightarrow S(X, Y, X) \quad (1)$$

$$a(X) \wedge r(X, Y) \rightarrow S(X, X, Y) \quad (2)$$

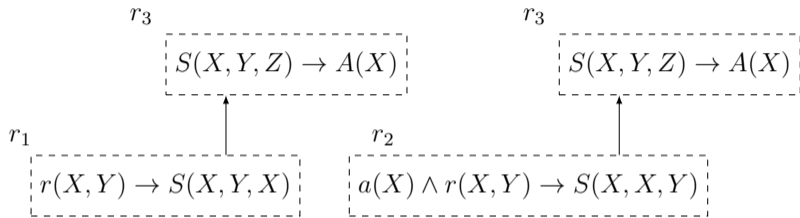
$$S(X, Y, Z) \rightarrow A(X) \quad (3)$$



Trigger Graphs for Datalog Rules: Example



Trigger Graph



$$Q(X) = \exists Y. r(X, Y)$$

Query for v_3

$$Q'(X) = \exists Y. a(X) \wedge r(X, Y)$$

Query for v_4

Trigger Graphs for Datalog Rules: Results

Let P be a Datalog program.

Theorem (Soundness)

For a TG G for P , $\text{minDatalog}(G)$ is a TG for P .

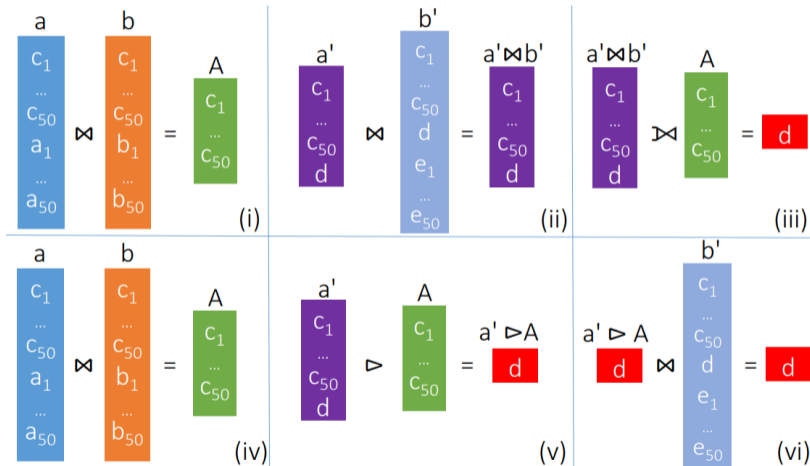
Theorem (Minimality)

Any TG for P has at least as many nodes as $\text{minDatalog}(G)$.

Theorem (Complexity)

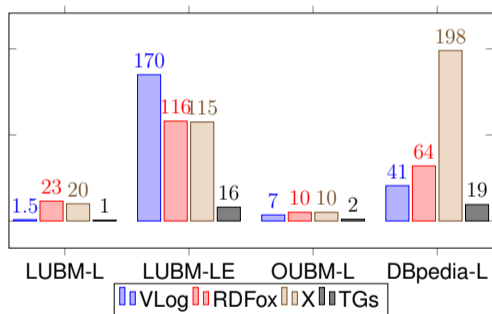
Deciding whether G is a TG of minimum size for P is co-NP-complete.

More: TG-Aware Rule Execution Strategy

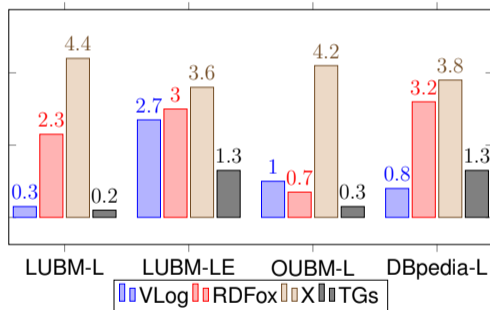


Datalog Reasoning with Trigger Graphs

Materialization times in s

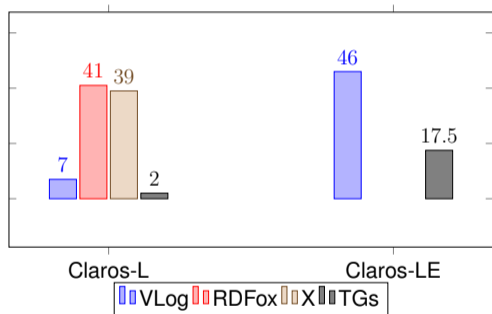


Pick memory in GB

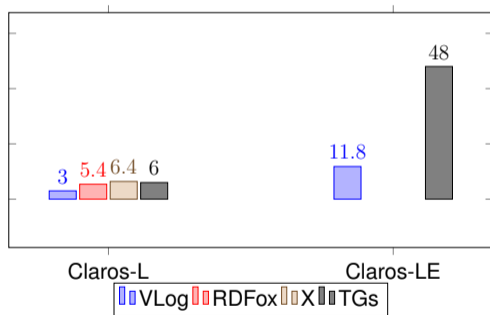


Datalog Reasoning with Trigger Graphs

Materialization times in minutes



Pick memory in GB



Reasoning at Scale: How -Lineage Trigger Graphs

Efthymia Tsamoura, Jaehun Lee, and Jacopo Urbani. **Probabilistic Reasoning as Scale: Trigger Graphs to the Rescue**. In SIGMOD, 2023 (*to appear*).

Aim

- Develop highly-scalable reasoning techniques that support uncertainty.
- Adopt well-established semantics.

Key Challenge: Complexity

Rules

$$e(X, Y) \rightarrow p(X, Y)$$

$$p(X, Z) \wedge p(Z, Y) \rightarrow p(X, Y)$$

Facts

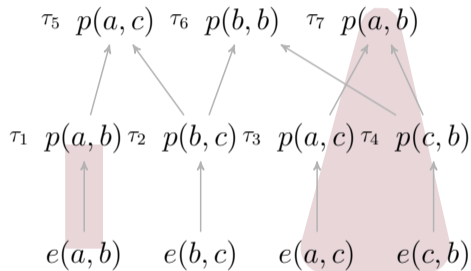
$$\rightarrow e(a, b)$$

$$\rightarrow e(a, c)$$

$$\rightarrow e(b, c)$$

$$\rightarrow e(c, b)$$

Derivations



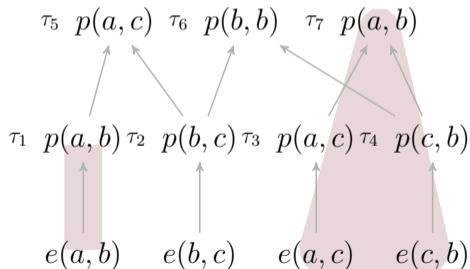
Prior Art: Key Limitations

- Relies on provenance semirings [9], i.e., associates a Boolean formula to each derivation.
- Super-polynomial size blowup in data complexity: *any monotone formula to test connectivity in a graph with n nodes has size $n^{\Omega(\log n)}$ (lower bound holds even for undirected graphs) [12].*
- Requires Boolean checks at each reasoning step for termination.
 - Runtime bottleneck.

Efthymia Tsamoura, Victor Gutierrez-Basulto, and Angelika Kimmig. Beyond the Grounding Bottleneck: Datalog Techniques for Inference in Probabilistic Logic Programs. In AAI, pages 10284-10291, 2020.

Probabilistic Reasoning via Provenance Semirings

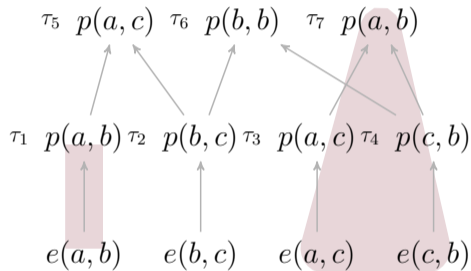
R	Derivation@R	Comparison	Formula@R
1	$e(a, b)$	\emptyset	$e(a, b)$
2	$e(a, c) \wedge e(c, b)$	$e(a, c) \wedge e(c, b) \stackrel{?}{\equiv} e(a, b)$	$e(a, c) \wedge e(c, b) \vee e(a, b)$



Lineage Trigger Graphs

- Efficient maintenance of derivation history.
- Natural for TGs.
- Storing pointer offsets.
- Reduces termination checks for detecting cyclic derivations!
 - No Boolean checks are required!

Derivations



Lineage Trigger Graphs: (Adaptive) Provenance Circuits

- Extended the notion of provenance circuits [5] to allow a more space-efficient reasoning:
 - Polynomial size representation.

Probabilistic Datalog Reasoning with Trigger Graphs

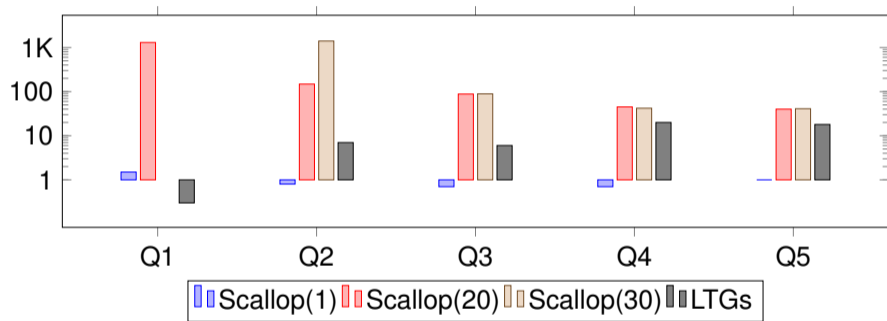


Figure: Time in seconds for goal-driven QA over sample queries from VQAR [11].

Conclusions++

Cool Research not Covered: Goal-driven QA over existential rules with equality (AAAI 2018)

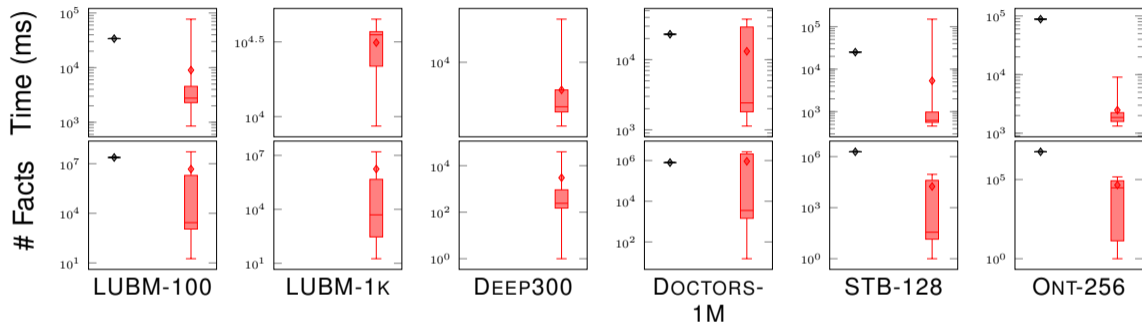


Figure: Time in msec to answer the ChaseBench queries [2].

Michael Benedikt, Boris Motik, and Efhymia Tsamoura. Goal-Driven Query Answering over Existential Rules with Equality. In AAAI, pages 1761–1770, 2018.

Cool Research not Covered: PRISM (AAAI 2023)

- **Objective:** mining rule patterns under (ϵ, α) -guarantees:
 - ϵ controls the uncertainty in the entity similarity measure;
 - α controls the softness of the resulting rules.
- Runtime optimality for given ϵ .
- $O(n \log n)$ vs. $O(n^3)$ (in the size of the entities in the data) algorithm for clustering structurally-related data.
- PRISM outperforms SOTA by up to **6%** in accuracy and up to 80% in runtime.

Leon Jonathan Feldstein, Dominic Phillips and **Efthymia Tsamoura**. **Principled and Efficient Motif Finding for Structure Learning of Lifted Graphical Models**. In AAAI, 2023.


Keywords (instead of conclusions)


- Uncertainty— many proposals, what is the right semantics?
- Formal guarantees.


Thanks!

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